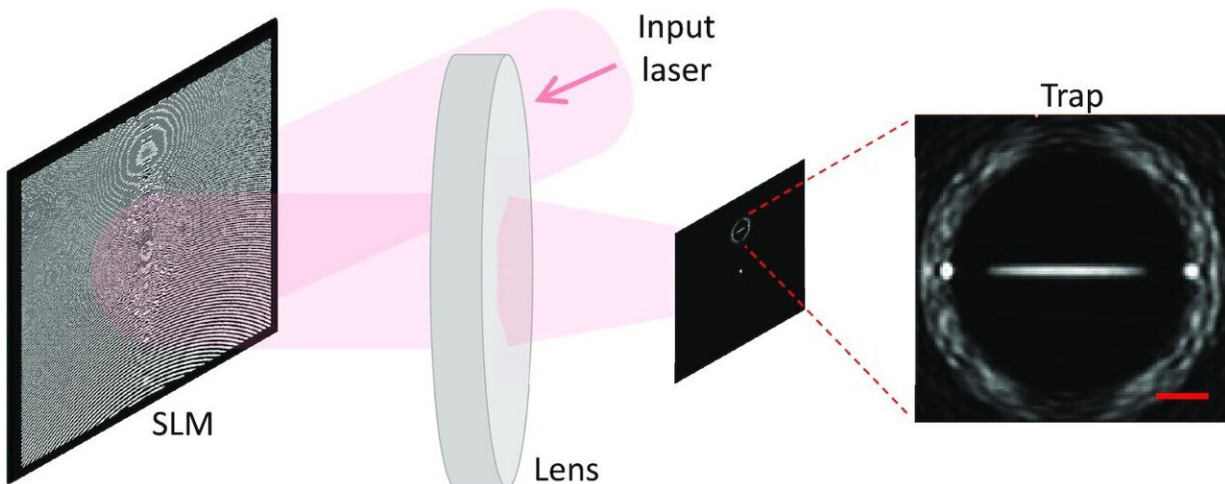


The first lab-created 'quantum abacus'

February 2 2023



Experimental setup, showing the phase profile imprinted by the SLM and the resulting light intensity profile in the trapping plane. The zoomed-in image shows the SR, i.e. the region of the output plane in which the field is programmed by the conjugate gradient minimization algorithm. In this case, the SR contains a generic 1D trapping potential. The circular intensity distribution delimitates the boundary with the region of the output plane where the intensity is left unconstrained. The scale bar is 100 μm . *PNAS Nexus* (2022). DOI: 10.1093/pnasnexus/pgac279

Do you want to know whether a very large integer is a prime number or not? Or if it is a "lucky number"? A new study by SISSA, carried out in collaboration with the University of Trieste and the University of Saint Andrews, suggests an innovative method that could help answer such questions through physics, using some sort of "quantum abacus."

By combining theoretical and [experimental work](#), scientists were able to reproduce a quantum potential with [energy levels](#) corresponding to the first 15 [prime numbers](#) and the first 10 lucky numbers using holographic laser techniques. This result, published in *PNAS Nexus*, opens the door to obtaining potentials with finite sequences of integers as arbitrary quantum energies, and to addressing mathematical questions related to [number theory](#) with quantum mechanical experiments.

"Every physical system is characterized by a certain set of energy levels, which basically make up its ID," explains Giuseppe Mussardo, [theoretical physicist](#) at SISSA—International School for Advanced Studies. "In this work, we have reversed this line of reasoning: is it possible—starting from an arithmetic sequence, for example that of prime numbers—to obtain a quantum system with those very numbers as energy levels?"

The answer is yes, as shown by the study published in *PNAS Nexus*. The researchers applied a system of differential equations to calculate the potential appearing in the Schrödinger equation of a quantum system, whose energy states correspond to a finite sequence of integers, extracted from a specific series, such as prime numbers or the close lucky numbers. Using sophisticated holographic experimental techniques, they were then able to create light traps with intensity profiles corresponding to the theoretically-defined potential.

"So far, we have calculated and created in the laboratory the quantum potential based on the first 15 prime numbers and the first 10 lucky numbers," added Giuseppe Mussardo, "but the same approach could be applied, in principle, to other—even infinitely long—number sequences, as long as the numbers don't grow too fast. More precisely, the growth of the infinite sequence needs to be less than N^2 ."

The experimental part of the work required the use of complex

holographic techniques and was performed by Donatella Cassettari's team at the University of Saint Andrews. "The realization of these quantum potentials is a stringent test of the holographic techniques that have recently been developed by my team," said the researcher.

"This study shows that complex intensity profiles can be realized with good accuracy. Many interesting directions can be taken based on these results, for example potentials with a greater number of energy levels. In the future, testing the limit of these techniques will also be interesting."

"Our work shows the feasibility of this method and paves the way for the exploration of genuine mathematical issues and arithmetical manipulations through [quantum mechanics](#) experiments: a kind of 'quantum abacus,'" notes Andrea Trombettoni, physicist at the University of Trieste.

"The method used and its possible generalizations may also lead to new applications in the field of quantum technology, which is currently the focus of much work and interest. Indeed, it provides a possible basic ingredient for a new class of devices, in which new algorithms that are relevant to quantum technologies—particularly quantum computing—can be designed and tested," concluded the researcher.

More information: Donatella Cassettari et al, Holographic realization of the prime number quantum potential, *PNAS Nexus* (2022). [DOI: 10.1093/pnasnexus/pgac279](https://doi.org/10.1093/pnasnexus/pgac279)

Provided by International School of Advanced Studies (SISSA)

Citation: The first lab-created 'quantum abacus' (2023, February 2) retrieved 26 April 2024 from <https://phys.org/news/2023-02-lab-created-quantum-abacus.html>

This document is subject to copyright. Apart from any fair dealing for the purpose of private study or research, no part may be reproduced without the written permission. The content is provided for information purposes only.