

## A first step towards quantum algorithms: Minimizing the guesswork of a quantum ensemble

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The paper provides analytical solutions for quantum ensembles with uniform probability distribution, qubit regular polygon ensembles, and qubit regular polyhedral ensembles. Credit: Waseda University

Given the rapid pace at which technology is developing, it comes as no surprise that quantum technologies will become commonplace within decades. A big part of ushering in this new age of quantum computing requires a new understanding of both classical and quantum information and how the two can be related to each other.



Before one can send classical information across quantum channels, it needs to be encoded first. This encoding is done by means of quantum ensembles. A quantum ensemble refers to a set of quantum states, each with its own probability. To accurately receive the transmitted information, the receiver has to repeatedly 'guess' the state of the information being sent. This constitutes a cost function that is called 'guesswork.' Guesswork refers to the average number of guesses required to correctly guess the state.

The concept of guesswork has been studied at length in classical ensembles, but the subject is still new for quantum ensembles. Recently, a research team from Japan—consisting of Prof. Takeshi Koshiba of Waseda University, Michele Dall'Arno from Waseda University and Kyoto University, and Prof. Francesco Buscemi from Nagoya University—has derived analytical solutions to the guesswork problem subject to a finite set of conditions. "The guesswork problem is fundamental in many scientific areas in which machine learning techniques or artificial intelligence are used. Our results trailblaze an algorithmic aspect of the guesswork problem," says Koshiba. Their findings are published in *IEEE Transactions on Information Theory*.

To begin with, the researchers considered a common formalism of quantum circuits that relates the transmitted state of a quantum ensemble  $\rho$  to the quantum measurement  $\pi$ . They next introduced the probability distributions for both the quantum ensemble and the numberings obtained from the quantum measurement. They then established the guesswork function. The guesswork function maps any pair of  $\rho$  and  $\pi$  into the expectation value of the t<sup>th</sup> guess (where t refers to the guess number), averaged over the probability distribution of the t<sup>th</sup> guess being correct. Finally, they minimized the guesswork function over the elements of  $\pi$  and used this result to derive analytical solutions to the guesswork problem subject to a finite set of conditions.



These solutions included the explicit solution to a qubit ensemble with a uniform probability distribution. "Previously, results for analytical solutions have been known only for binary and symmetric ensembles. Our calculation for ensembles with a uniform probability distribution extends these," explains Koshiba. The research team also calculated the solutions for a qubit regular polygonal ensemble, and a qubit regular polyhedral ensemble.

"Guesswork is a very basic scientific problem, but there is very little research on quantum guesswork and even less on the algorithmic implications of quantum guesswork. Our paper goes a little way towards filling that gap," concludes Koshiba.

While the consequences of these findings may not be immediately obvious, in the future they are sure to have a major influence on quantum science, such as quantum chemistry for drug development and quantum software for quantum computing.

**More information:** Michele Dall'Arno et al, Guesswork of a quantum ensemble, *IEEE Transactions on Information Theory* (2022). DOI: 10.1109/TIT.2022.3146463

Provided by Waseda University

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