

The weird world of one-sided objects

September 24 2018, by David Gunderman And Richard Gunderman



Credit: AI-generated image ([disclaimer](#))

You have most likely encountered one-sided objects hundreds of times in your daily life – like the [universal symbol](#) for recycling, found printed on the backs of aluminum cans and plastic bottles.

This [mathematical object](#) is called a Mobius strip. It has fascinated environmentalists, artists, engineers, mathematicians and many others ever since its discovery in 1858 by August Möbius, a German

mathematician who died 150 years ago, on Sept. 26, 1868.

[Möbius](#) discovered the one-sided strip in 1858 while serving as the chair of astronomy and higher mechanics at the University of Leipzig. (Another mathematician named Listing actually described it a few months earlier, but did not publish his work until 1861.) Möbius seems to have encountered the Möbius strip while working on the geometric theory of polyhedra, solid figures composed of vertices, edges and flat faces.

A Möbius strip can be created by taking a strip of paper, giving it an odd number of half-twists, then taping the ends back together to form a loop. If you take a pencil and draw a line along the center of the strip, you'll see that the line apparently runs along both sides of the loop.

The concept of a one-sided object inspired artists like Dutch graphic designer [M.C. Escher](#), whose woodcut "[Möbius Strip II](#)" shows red ants crawling one after another along a Möbius strip.

The Möbius strip has more than just one surprising property. For instance, try taking a pair of scissors and cutting the strip in half along the line you just drew. You may be astonished to find that you are left not with two smaller one-sided Möbius strips, but instead with one long two-sided loop. If you don't have a piece of paper on hand, Escher's woodcut "[Möbius Strip I](#)" shows what happens when a Möbius strip is cut along its center line.

While the strip certainly has visual appeal, its greatest impact has been in mathematics, where it helped to spur on the development of an entire field called [topology](#).

A topologist studies properties of objects that are preserved when moved, bent, stretched or twisted, without cutting or gluing parts

together. For example, a tangled pair of earbuds is in a topological sense the same as an untangled pair of earbuds, because changing one into the other requires only moving, bending and twisting. No cutting or gluing is required to transform between them.

Another pair of objects that are topologically the same are a coffee cup and a doughnut. Because both objects have just one hole, one can be deformed into the other through just stretching and bending.



A mug morphs into a doughnut. Credit: Wikimedia Commons

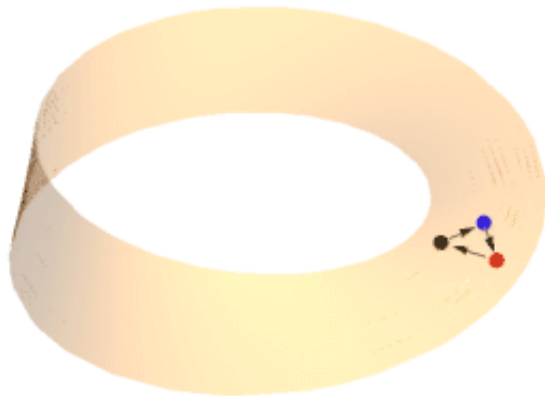
The number of holes in an object is a property which can be changed only through cutting or gluing. This property – called the "genus" of an object – allows us to say that a pair of earbuds and a doughnut are topologically different, since a doughnut has one hole, whereas a pair of earbuds has no holes.

Unfortunately, a Möbius strip and a two-sided loop, like a typical silicone awareness wristband, both seem to have one hole, so this

property is insufficient to tell them apart – at least from a topologist's point of view.

Instead, the property that distinguishes a Möbius strip from a two-sided loop is called orientability. Like its number of holes, an object's orientability can only be changed through cutting or gluing.

Imagine writing yourself a note on a see-through surface, then taking a walk around on that surface. The surface is orientable if, when you come back from your walk, you can always read the note. On a nonorientable surface, you may come back from your walk only to find that the words you wrote have apparently turned into their mirror image and can be read only from right to left. On the two-sided loop, the note will always read from left to right, no matter where your journey took you.



When the GIF starts, the dots listed off clockwise are black, blue and red. However, we can move the three-dot configuration around the Möbius strip such that the figure is in the same location, but the colors of the dots listed off clockwise are now red, blue and black. Somehow, the configuration has morphed into its own mirror image, but all we've done is move it around on the surface. This transformation is impossible on an orientable surface like the two-sided

loop. Credit: David Gunderman.

Since the Möbius strip is nonorientable, whereas the two-sided loop is orientable, that means that the Möbius strip and the two-sided loop are topologically different.

The concept of orientability has important implications. Take enantiomers. These chemical compounds have the same chemical structures except for one key difference: They are mirror images of one another. For example, [the chemical L-methamphetamine](#) is an ingredient in Vicks Vapor Inhalers. Its mirror image, D-methamphetamine, is a Class A illegal drug. If we lived in a nonorientable world, these chemicals would be indistinguishable.

August Möbius's discovery opened up new ways to study the natural world. The study of topology continues to produce stunning results. For example, last year, topology led scientists to discover [strange new states of matter](#). This year's Fields Medal, the highest honor in mathematics, [was awarded to Akshay Venkatesh](#), a mathematician who helped integrate topology with other fields such as number theory.

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