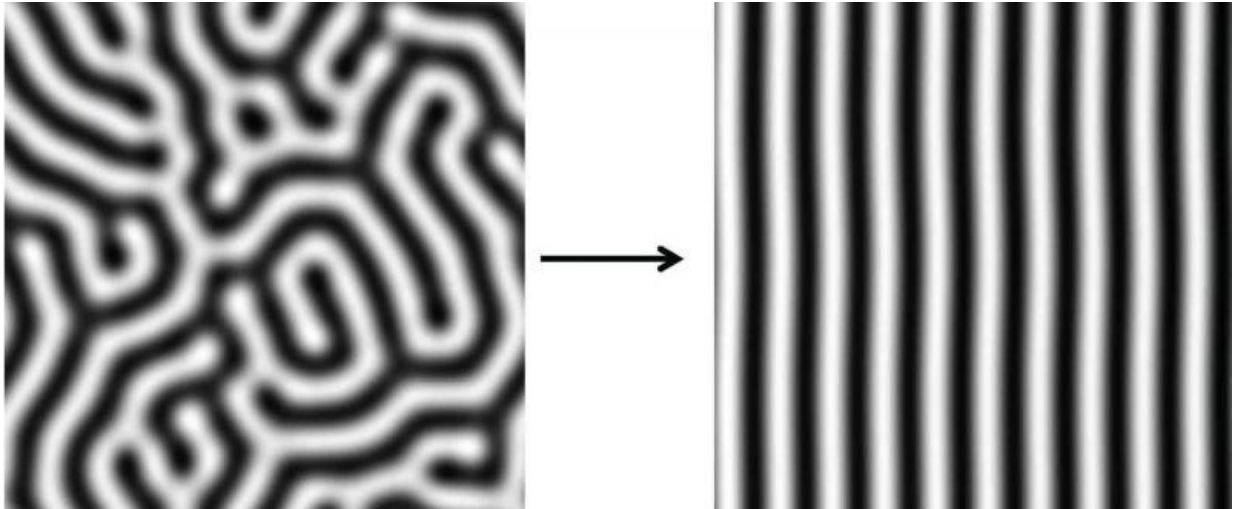


# A mathematical model for animal stripes

December 23 2015

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Simulations of Turing stripes. On the left, stripes are evenly spaced, but their direction is variable. On the right, a signaling gradient has made the stripes align in the same direction. Credit: Tom Hiscock

The back of a tiger could have been a blank canvas. Instead, nature painted the big cat with parallel stripes, evenly spaced and perpendicular to the spine. Scientists don't know exactly how stripes develop, but since the 1950s, mathematicians have been modeling possible scenarios. In *Cell Systems* on December 23, Harvard researchers assemble a range of these models into a single equation to identify what variables control stripe formation in living things.

"We wanted a very simple [model](#) in hopes that it would be big picture

enough to include all of these different explanations," says lead author Tom Hiscock, a PhD student in Sean Megason's systems biology lab at Harvard Medical School. "We now get to ask what is common among molecular, cellular, and mechanical hypotheses for how living things orient the directions of stripes, which can then tell you what kinds of experiments will (or won't) distinguish between them."

Stripes are surprisingly simple to model mathematically (and much of the early work on the subject was by Alan Turing of "The Imitation Game" fame). These patterns emerge when interacting substances create waves of high and low concentrations of, for example, a pigment, chemical, or type of cell. What Turing's model doesn't explain is how stripes orient themselves in one particular direction.

Hiscock's investigation focused on orientation—e.g., why tiger stripes are perpendicular to its body while zebrafish stripes are horizontal. One surprise from his integrated model is that it takes only a small change to the model to switch whether the stripes are vertical or horizontal. What we don't know is how this translates to living things—so, for a tiger, what is the variable that pushes the development of perpendicular stripes?

"We can describe what happens in stripe formation using this simple [mathematical equation](#), but I don't think we know the nitty-gritty details of exactly what molecules or cells are mapping the formation of stripes," Hiscock says. Genetic mutants exist that can't form stripes or make spots instead, such as in zebrafish, but "the problem is you have a big network of interactions, and so any number of parameters can change the pattern," he adds.

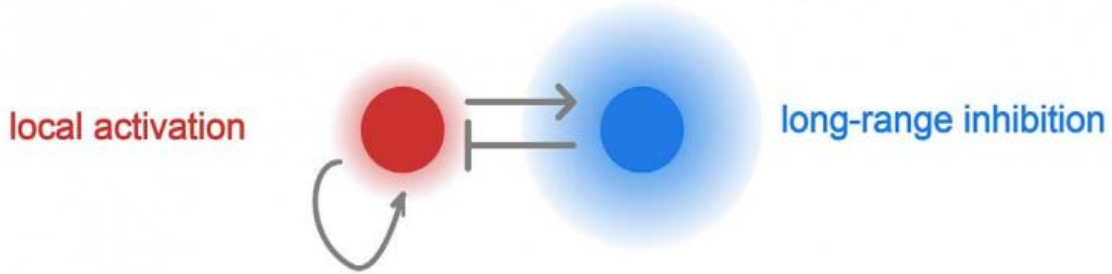
$$\frac{\partial \phi}{\partial t} = a(\mathbf{x})\phi - \mathcal{L}(\partial_x^2, \partial_y^2)\phi - d\phi^3 + h(\mathbf{x})$$

An equation assembling multiple hypotheses for how Turing-like stripes are oriented. Credit: Hiscock and Megason/*Cell Systems* 2015

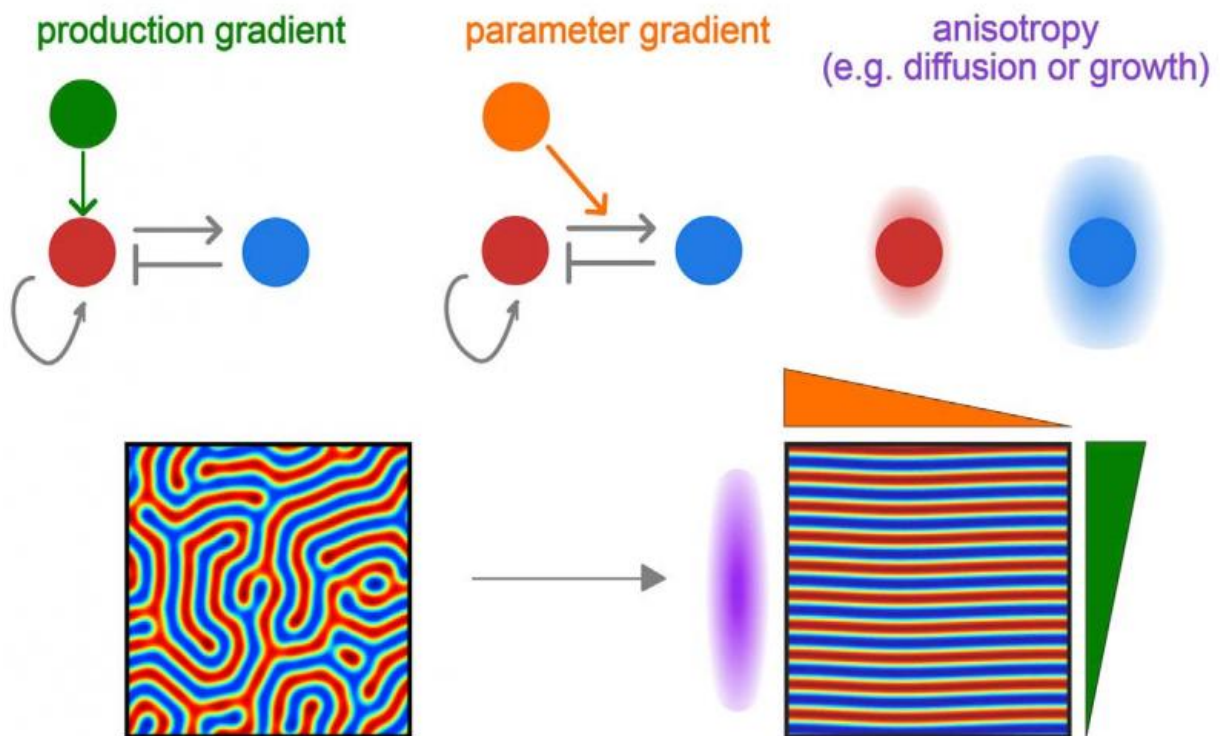
His master model predicts three main perturbations that can affect how stripes orient: one is a change in "production gradient," which would be a substance that amplifies stripe pattern density; second is a change in "parameter gradient," a substance that changes one of the parameters involved in forming the stripe; and the last is a physical change in the direction of the molecular, cellular, or mechanical origin of the stripe.

Although this paper is based in theory, Hiscock believes that we are close to having the experimental tools that can decipher whether the math holds true in living systems.

## What orients stripes in a Turing pattern?



Theory predicts three qualitatively distinct mechanisms:



How do developmental programs ensure that stripes patterns always point in the same direction (e.g., what makes the fingers form parallel to the arm)? This graphical abstract shows how a simple model of Turing stripe formation predicts three distinct ways to orient stripes that apply to a wide variety of biological mechanisms. Credit: Hiscock and Megason/*Cell Systems* 2015

**More information:** *Cell Systems*, Hiscock and Megason: "Orientation of Turing-like Patterns by Morphogen Gradients and Tissue Anisotropies," [dx.doi.org/10.1016/j.cels.2015.12.001](https://doi.org/10.1016/j.cels.2015.12.001)

Provided by Cell Press

Citation: A mathematical model for animal stripes (2015, December 23) retrieved 12 September 2024 from <https://phys.org/news/2015-12-mathematical-animal-stripes.html>

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